

ECE 473  
Homework Assignment #11  
Due: Wednesday, December 12, 2018

1. Consider an infinitely long rigid-walled pipe of rectangular cross section of dimensions  $L_x = 0.5$  m and  $L_y = 0.7$  m and filled with water at  $20^\circ\text{C}$ . Find the cutoff frequencies for the lowest five modes.
2. A pipe is 0.02 m in radius and 2 m long. (a) Determine the three lowest resonance frequencies if the pipe is filled with air at  $20^\circ\text{C}$  and has a rigid cap at its end. (b) Determine the three lowest resonance frequencies if the pipe is filled with water at  $20^\circ\text{C}$  and has a rigid cap at its end. (c) Determine the three lowest resonance frequencies if the pipe is filled with air at  $20^\circ\text{C}$  and has a flanged opening at its end.
3. An acoustical tile is placed at the end of a pipe with radius small compared to the wavelength. At the beginning of the pipe a piston is used to generate a 200 Hz acoustic plane wave. A very small microphone is inserted into the pipe via a small slot in the bottom so that it can be moved and used to measure the pressure amplitude as a function of distance from the end ( $x = L$ ), without affecting the acoustic field. Using the microphone a standing wave ratio of 12 is measured and the first pressure minimum is found to be 0.4 m from the end ( $x = L$ ). (a) What are the magnitude and polar angle for the complex reflection coefficient,  $\tilde{B}/\tilde{A}$ ? (b) What is the normal specific acoustic impedance of the acoustic tile?
4. For an open ended unflanged pipe, show that the half-power points (frequencies) are given by  $\omega_{u,1} = \omega_n \pm \frac{1}{4}(k_n a)^2 \frac{c}{L}$  and that  $Q_n = \frac{\omega_n}{\omega_u - \omega_l} = \frac{2}{n\pi} \frac{L}{a} \frac{L + 0.6a}{a}$ .
5. A section of pipe of cross-sectional area  $0.4$  m<sup>2</sup> and length  $0.3$  m is in a pipe of cross-sectional area  $0.2$  m<sup>2</sup>. (a) Over what frequency range will the larger cross-section of pipe act as a low pass filter? (b) What is the maximum attenuation it provides, in decibels?

**Note to graduate students writing the paper:** For the additional credit, you are required to write a paper (typically about 10 pages, double spaced) that discusses in some detail any topic on acoustics for which the fundamentals of engineering acoustics are explicitly described. The paper is typically a summary of some acoustic topic and based on 4-5 peer-reviewed publications. The paper will be due **Dec 12, 2018**.